

For 3D math,

What is the term for  
a generalized  
**cross product**?

3D Math

Given vectors  $\mathbf{a}$  and  $\mathbf{b}$   
what is the return of  
their cross product,  
 $\mathbf{a} \times \mathbf{b}$ ?

3D Math

Given vectors  $\mathbf{a}$  and  $\mathbf{b}$   
what operation calculates  
a new vector **perpendicular**  
to both  $\mathbf{a}$  and  $\mathbf{b}$ ?

3D Math

Given the 3D vectors  
 $\mathbf{u}$  and  $\mathbf{v}$ ,  
what does the equation  
below return?

$$\cos^{-1}\left(\frac{\mathbf{u} \cdot \mathbf{v}}{|\mathbf{u}| |\mathbf{v}|}\right)$$

3D Math

Given the 3D vectors  
 $\mathbf{v}$  and  $\mathbf{u}$ ,  
what does the equation  
below return?

$$\cos^{-1}(\|\mathbf{u}\| \cdot \|\mathbf{v}\|)$$

3D Math

Given the 3D vectors  
 $\mathbf{u}$  and  $\mathbf{v}$ ,  
what formula calculates  
the angle between them?

3D Math

Given 3D vectors  $\mathbf{a}$  and  $\mathbf{b}$ ,  
each with elements  $x, y, z$ ,  
formulate the dot product  
between them.

3D Math

For 3D math,

Given the dot product:  
 $\mathbf{a} \cdot \mathbf{b}$

What is the **magnitude**  
of the value returned?

3D Math

Given the 3D vectors  $\mathbf{v}$ ,  
what's the value from  
dot producing it with  
a perpendicular vector?

$$\mathbf{u} \cdot \perp \mathbf{u}$$

3D Math

For 3D math,

What is another term  
for  
**projection product**?

3D Math

$$n \|\mathbf{a}\| \|\mathbf{b}\| \sin \theta$$

Where  $\theta$  is the angle between  $\mathbf{a}$  and  $\mathbf{b}$ .  
 Where  $n$  is an angle perpendicular to  $\mathbf{a}$  and  $\mathbf{b}$ .  
 $n = \perp(\|\mathbf{a}\| \|\mathbf{b}\|)$

A wedge product.

The angle between  
 $\mathbf{u}$  and  $\mathbf{v}$ .

The angle will be in radians

$$\frac{\cos^{-1}(\|\mathbf{u}\| \cdot \|\mathbf{v}\|)}{\text{OR}} \frac{\cos^{-1}\left(\frac{\mathbf{u} \cdot \mathbf{v}}{\|\mathbf{u}\| \|\mathbf{v}\|}\right)}$$

The angle will be in radians.

Cross Product

With the notation:  $\mathbf{a} \times \mathbf{b}$

The angle between  
 $\mathbf{u}$  and  $\mathbf{v}$ .

The angle will be in radians

$$\|\mathbf{a}\| \|\mathbf{b}\| \cos \theta$$

Their magnitudes multiplied,  
 scaled by the cos of the angle  
 between the vectors.

$$\mathbf{a}_x \mathbf{b}_x + \mathbf{a}_y \mathbf{b}_y + \mathbf{a}_z \mathbf{b}_z$$

- Dot Product, or
- Inner Product, or
- Scalar Product

For 3D math,

What is another term for  
**dot product**?

3D Math

For 3D math,

What is another term for  
**inner product**?

3D Math

For 3D math,

What is another term for  
**scalar product**?

3D Math

For 3D math,

What is the **generalized**  
form of the  
**dot product** equation  
called?

3D Math

Given the 3D vectors  $\mathbf{v}$ ,  
whats the value from  
dot-producing  
its normal with its normal?

$$\|\mathbf{u}\| \cdot \|\mathbf{u}\|$$

3D Math

Given the 3D vectors  $\mathbf{v}$ ,  
whats the value from  
dot-producing  
its normal with  
its negated normal?

$$\|\mathbf{u}\| \cdot -\|\mathbf{u}\|$$

3D Math

Given vectors  $\mathbf{v}_1$  and  $\mathbf{v}_2$ ,  
and value  $t$  between  $[0,1]$ ,  
What is the **formula**  
for **linear interpolation**?

3D Math

For Linear Algebra,

What does the term  
**lerp**  
stand for?

3D Math

What does the  
determinant of a matrix  
represent?

3D Math

When **inverting** a **matrix**,  
what happens if  
its **determinant** is **zero**?

3D Math

- Dot Product, or
- Projection Product, or
- Scalar Product

- Projection Product, or
- Inner Product, or
- Scalar Product

Inner Product

- Dot Product, or
- Projection Product, or
- Inner Product

-1

1

Linear interpolation.

$$\mathbf{v}_1 + (\mathbf{v}_2 - \mathbf{v}_1) * t$$

OR

$$\mathbf{v}_1 * (1-t) + \mathbf{v}_2 * t$$

A zero determinant means the matrix cannot be inverted.

The volume inside the matrix.

If each column represented a vector that represented an edge of a box/(hyper)cube, it represents what the volume of that cube would be.

(For matrices representing more than 3 dimensions, technically it's the *hyper-volume*)

What does the determinant of a matrix represent?

3D Math

If a **matrix** has either **all zeros** for any **column** or **all zeros** for any **row**, What does that tell you about its **determinant**?

3D Math

Given a 1D matrix **A**, with members:

$$\begin{bmatrix} a_1 \end{bmatrix}$$

what is its **determinant**?

3D Math

Given a 2D matrix **A**, with members:

$$\begin{bmatrix} u_1 & v_1 \\ u_2 & v_2 \end{bmatrix}$$

what is its determinant?

3D Math

Given a 2D matrix **A**, with members:

$$\begin{bmatrix} u_1 & v_1 & w_1 \\ u_2 & v_2 & w_2 \\ u_3 & v_3 & w_3 \end{bmatrix}$$

what is its determinant?

3D Math

Given a matrix **A**, what does the **notation**  $|\mathbf{A}|$  mean?

3D Math

Given a matrix **A**, what does the notation  $\det(\mathbf{A})$  mean?

3D Math

Given a matrix **A** of size  $m \times n$ , how many **columns** and **rows** does the matrix have?

3D Math

Given a matrix **A** of size  $m \times n$ , how many **rows** and **columns** does the matrix have?

3D Math

Given a matrix **A**, what does the **notation**  $\mathbf{A}^{-1}$  mean?

3D Math

The determinant will be zero.

$$u_1v_2 - u_2v_1$$

The determinant of matrix **A**.

$m$  rows  
 $n$  columns

The **inverse** of matrix **A**.

The volume inside the matrix.

i.e., if each column represented a vector that represented an edge of a box/(hyper)cube, it represents what the volume of that cube would be.

(For matrices representing more than 3 dimensions, technically it's the *hyper-volume*)

$$a_1$$

$$u_1(v_2v_3 - v_3v_2) + u_2(v_3v_1 - v_1v_3) + u_3(v_1v_2 - v_2v_1)$$

The determinant of matrix **A**.

$m$  rows  
 $n$  columns

Given a matrix  $A$ ,  
what's the **notation**  
to represent its **inverse**?

3D Math

Given a 2D matrix  $A$ ,  
with members:

$$\begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix}$$

what is its **inverse**?

3D Math

Given a 3D matrix  $A$ ,  
with members:

$$\begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix}$$

what is its **inverse**?

3D Math

For a 3D matrix,  
what does it mean if we  
orthonormalize it?

3D Math

For a 3D matrix,  
what does it mean if we  
say it's skewed?

3D Math

Given a 2D matrix  $A$ ,  
what does the notation  
 $A^T$   
mean?

3D Math

Given a 2D matrix  $A$ ,  
what's the notation  
to represent its **transpose**?

3D Math

Given a value  
 $x$  between  $[0, 1]$ ,  
give the formula for  
a **7th order**  
**smoothstep**.

3D Math

Given a value  
 $x$  between  $[0, 1]$ ,  
give the formula for  
**smootherstep**.

AKA: A 5th order smoothstep.

3D Math

Given a value  
 $x$  between  $[0, 1]$ ,  
give the formula for  
**smoothstep**.

3D Math

$$\frac{1}{\det(\mathbf{A})} \begin{bmatrix} a_{22} & -a_{12} \\ -a_{21} & a_{11} \end{bmatrix}$$

$$\mathbf{A}^{-1}$$

The matrix will be "corrected" so that:

- all 3 orientation vectors are **perpendicular** to each other
- all 3 orientation vectors are **unit** length.

$$\frac{1}{\det(\mathbf{A})} \begin{bmatrix} a_{22}a_{33}-a_{23}a_{32} & a_{13}a_{32}-a_{12}a_{33} & a_{12}a_{23}-a_{13}a_{22} \\ a_{23}a_{31}-a_{21}a_{33} & a_{11}a_{33}-a_{13}a_{31} & a_{13}a_{21}-a_{11}a_{23} \\ a_{21}a_{32}-a_{22}a_{31} & a_{12}a_{31}-a_{11}a_{32} & a_{11}a_{22}-a_{12}a_{21} \end{bmatrix}$$

(Note the pattern more than the actual values)

The **transpose** of matrix  $\mathbf{A}$ .

All 3 orientation vectors are not perpendicular to each other.

It can also be said the matrix is **not orthogonal**

$$-20x^7 + 70x^6 - 84x^5 + 35x^4$$

$$\mathbf{A}^T$$

$$3x^2 - 2x^3$$

$$6x^5 - 15x^4 + 10x^3$$

Given a value  $x$  between  $[0, 1]$ , give the formula for the **inverse** of a **cubic smoothstep**.

3D Math

For Linear Algebra,

What term is the generalization of a **matrix**?

3D Math

For Linear Algebra,

What are other terms for:  
1) A 1D tensor  
2) A 2D tensor

3D Math

What does the term **cubic** mean?

3D Math

What does the term **quadratic** mean?

3D Math

Given **3D** vectors  $\mathbf{a}$ ,  $\mathbf{b}$  and  $\mathbf{c}$ , what's the **difference** between their **tripple product** and the **determinant** of a matrix made by those vectors?

3D Math

Given the 3D vectors  $\mathbf{a}$ ,  $\mathbf{b}$  and  $\mathbf{c}$ , what does the notation  $[\mathbf{a} \ \mathbf{b} \ \mathbf{c}]$  represent?

3D Math

Given the 3D vectors  $\mathbf{a}$ ,  $\mathbf{b}$  and  $\mathbf{c}$ , what does the scalar tripple product  $(\mathbf{a} \times \mathbf{b}) \cdot \mathbf{c}$  represent?

3D Math

Given the 3D vectors  $\mathbf{a}$ ,  $\mathbf{b}$  and  $\mathbf{c}$ , what is the formula for the **volume** of the **tetrahedron** they form?

3D Math

Given 3D vectors  $\mathbf{a}$ ,  $\mathbf{b}$  and  $\mathbf{c}$ , what is the formula:  $(\mathbf{a} \times \mathbf{b}) \cdot \mathbf{c}$  called?

3D Math

A tensor.

$$\frac{1}{2} - \sin(\arcsin(1-2x)/3)$$

It involves a formula where a variable is raised to the **third power** - as the highest power.

- 1) A vector
- 2) A matrix

Nothing, they're equivalent.

It involves a formula where a variable is raised to the **second power** - as the highest power.

The volume of the parallelepiped formed by ***a***, ***b*** and ***c***.

The volume of the parallelepiped formed by ***a***, ***b*** and ***c***.

Which is also their determinant

Which is also their determinant  
aka, The Triple Product

Scalar triple product.

$$\frac{(\mathbf{a} \times \mathbf{b}) \cdot \mathbf{c}}{6}$$

Their scalar triple product divided by 6

Given the 3D vectors  $\mathbf{a}$ ,  $\mathbf{b}$  and  $\mathbf{c}$ , what is the formula for the scalar tripple product?

3D Math

Given a 3D vector  $\mathbf{v}$ , with the elements  $x, y, z$ , what is the formula to calculate its **magnitude**?

3D Math

Given a 3D vector  $\mathbf{v}$ , with the elements  $x, y, z$ , what is the formula to calculate its **length**?

3D Math

Given a vector  $\mathbf{v}$ , what does the notation  $|\mathbf{v}|$  mean?

3D Math

Given a vector  $\mathbf{v}$ , what **notation** represents the **magnitude** of the vector?

3D Math

Given a vector  $\mathbf{v}$ , what does the dot-product  $\mathbf{v} \cdot \mathbf{v}$  give back?

In respect to  $\mathbf{v}$   
3D Math

Given a 3D vector  $\mathbf{v}$ , with the elements  $x, y, z$ , what is the **formula** to **normalize** it?

3D Math

Given a vector  $\mathbf{v}$ , what does the notation  $\|\mathbf{v}\|$  represent?

3D Math

Given a vector  $\mathbf{v}$ , what does the notation

$\frac{\mathbf{v}}{|\mathbf{v}|}$   
represent?

3D Math

What does it mean if two **vectors** are **orthogonal** to each other?

3D Math

ANSWER

$$\sqrt{v_x^2 + v_y^2 + v_z^2}$$

The magnitude of the vector.

AKA: The Euclidean length

ANSWER

ANSWER

$$(a \times b) \cdot c$$

Operation is commutative, order of vectors does not matter.

ANSWER

$$\sqrt{v_x^2 + v_y^2 + v_z^2}$$

AKA: The vector magnitude formula

The magnitude squared of  $\mathbf{v}$ .

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$$\frac{|\mathbf{v}| \quad |\mathbf{v}|}{\text{AKA} \quad |\mathbf{v}|^2}$$

ANSWER

$$|\mathbf{v}|$$

The normalized value of  $\mathbf{v}$ .

AKA: The unit vector of  $\mathbf{v}$ .

ANSWER

$$\frac{\mathbf{v}}{\sqrt{v_x^2 + v_y^2 + v_z^2}}$$

It means they are perpendicular to each other.

ANSWER

The normalized value of  $\mathbf{v}$ .

AKA: The unit vector of  $\mathbf{v}$ .

What value **multiplier**  
converts  
**degrees**  
to  
**radians**?

3D Math

How many units of pi ( $\pi$ )  
represents 360 degrees?

3D Math

What value multiplier  
converts  
**radian**  
to  
**degrees**?

3D Math

Given vectors  $\mathbf{a}$  and  $\mathbf{b}$   
with elements  $x, y, z$ ,  
give the formula for a  
**cross product**.

The result vector will be called  $\mathbf{v}$ .

3D Math

Given 3D vectors  $\mathbf{a}$  and  $\mathbf{b}$   
what operation calculates  
the **area** a **triangle** with  
these vectors as the edges?

3D Math

When using the cross product,

if

$$\mathbf{a} \times \mathbf{b} = \mathbf{v},$$

what is the value of

$$\mathbf{b} \times \mathbf{a} = ?$$

3D Math

Given vectors  $\mathbf{a}$  and  $\mathbf{b}$   
what is the **identity** of the  
**magnitude** of their  
**cross product**?

3D Math

2

$\pi/180$

i.e.,  $2\pi = 360^\circ$

$$v_x = a_y b_z - a_z b_y$$

$$v_y = b_z a_x - a_x b_z$$

$$v_z = a_x b_y - a_y b_x$$

$180/\pi$

$-v$

$$\frac{|\mathbf{a} \times \mathbf{b}|}{2}$$

The cross product is not commutative.

Where  $\times$  is a cross product.  
( $|\mathbf{a} \times \mathbf{b}|$  returns the area of the parallelogram)

The area of the  
parallelepiped formed  
by  $\mathbf{a}$  and  $\mathbf{b}$ .

OR

$$|\mathbf{a}| |\mathbf{b}| \sin \theta$$

(Where  $\theta$  is the angle between  $\mathbf{a}$  and  $\mathbf{b}$ .)